

# SUSY CP Problem in Gauge Mediation Model

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# Supersymmetry

- SUSY is motivated by facts that SUSY ...
  - Solves the hierarchy problem
  - Preferred by gauge coupling unification
  - Provide a candidate for dark matter with R-parity

However ...

# SUSY CP Problem

In terms of the CP violation, soft SUSY breaking terms can cause trouble

Dangerous sources for CP violation

K-K  
bar  
mixing,  
EDM

squark mass  
(off-diagonal)

$$m_{\tilde{q}ij}$$

Higgs B-term

$$B_\mu$$

Gaugino  
masses

$$M_A$$

this  
talk

(The phases of A-terms are also relevant)

How to generate soft SUSY breaking parameters is  
important

# Gauge Mediation

Messenger

$$W = (M + F\theta^2)\Psi\bar{\Psi}$$

SUSY  
breaking

gaugino  $M_A \simeq \frac{g_A^2}{16\pi^2} \frac{F}{M}$

sfermion  $\tilde{m}_i^2 \simeq \frac{1}{(16\pi^2)^2} (c_A^i g_A^4) \left| \frac{F}{M} \right|^2$

real number

Both  $F$  and  $M$  can be taken to be real

No CPV in gaugino and sfermion masses

However, even in Gauge Mediation, new  
CPV phase can be induced

1. The phase of Higgs B-term

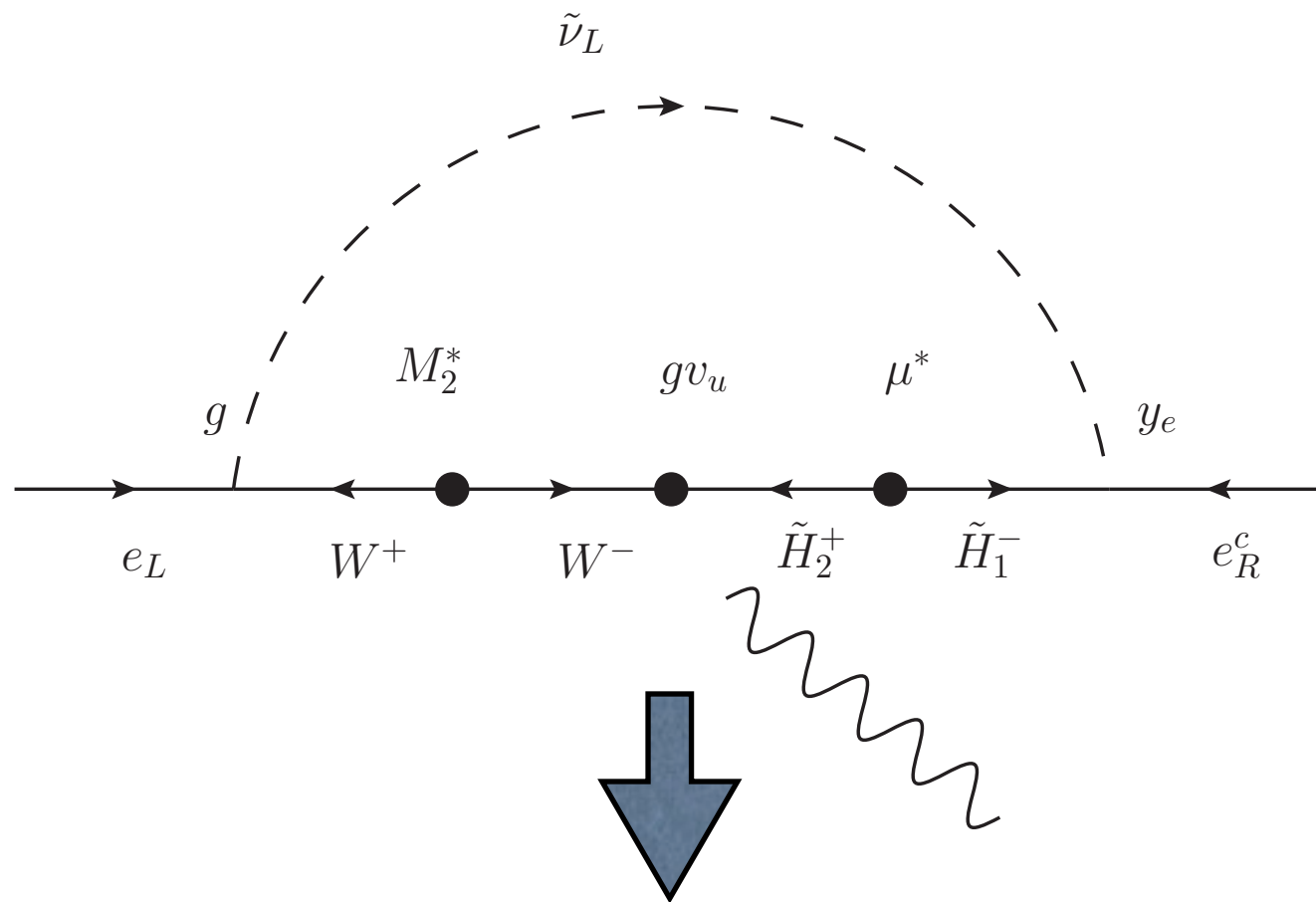
$\mu/B_\mu$   
problem

2. Small GUT breaking operator  
(Plank suppressed)

3. SUGRA effects

In this talk, we focus on 2 and 3

# Electric Dipole Moment



chargino diagram is  
dominant

(unless higgsino and  
wino are heavy)

$$d_e \propto m_e \tan \beta \operatorname{Arg}(M_2 B_\mu^*) / m_{soft}^2$$

exp. constraint

proportional to relative phase between  
Wino mass and Higgs B-term

$$d_e < 2.1 \times 10^{-27} e \text{ cm} \quad (95\% \text{ C.L.})$$

The phase should be small as  $O(10^{-3}-10^{-4})$  with  $O(1)$   
TeV sparticles and  $O(10) \tan \beta$

# Muon $g-2$

When sparticles are heavy the constraint on the phase becomes loose, however ....

The EXP value and SM prediction of muon  $g-2$  are deviated more than  $3\sigma$  level

$$a_{\mu}^{\text{EXP}} - a_{\mu}^{\text{SM}} = (26.1 \pm 8.0) \cdot 10^{-10} \quad 3.3\sigma \text{ deviation}$$

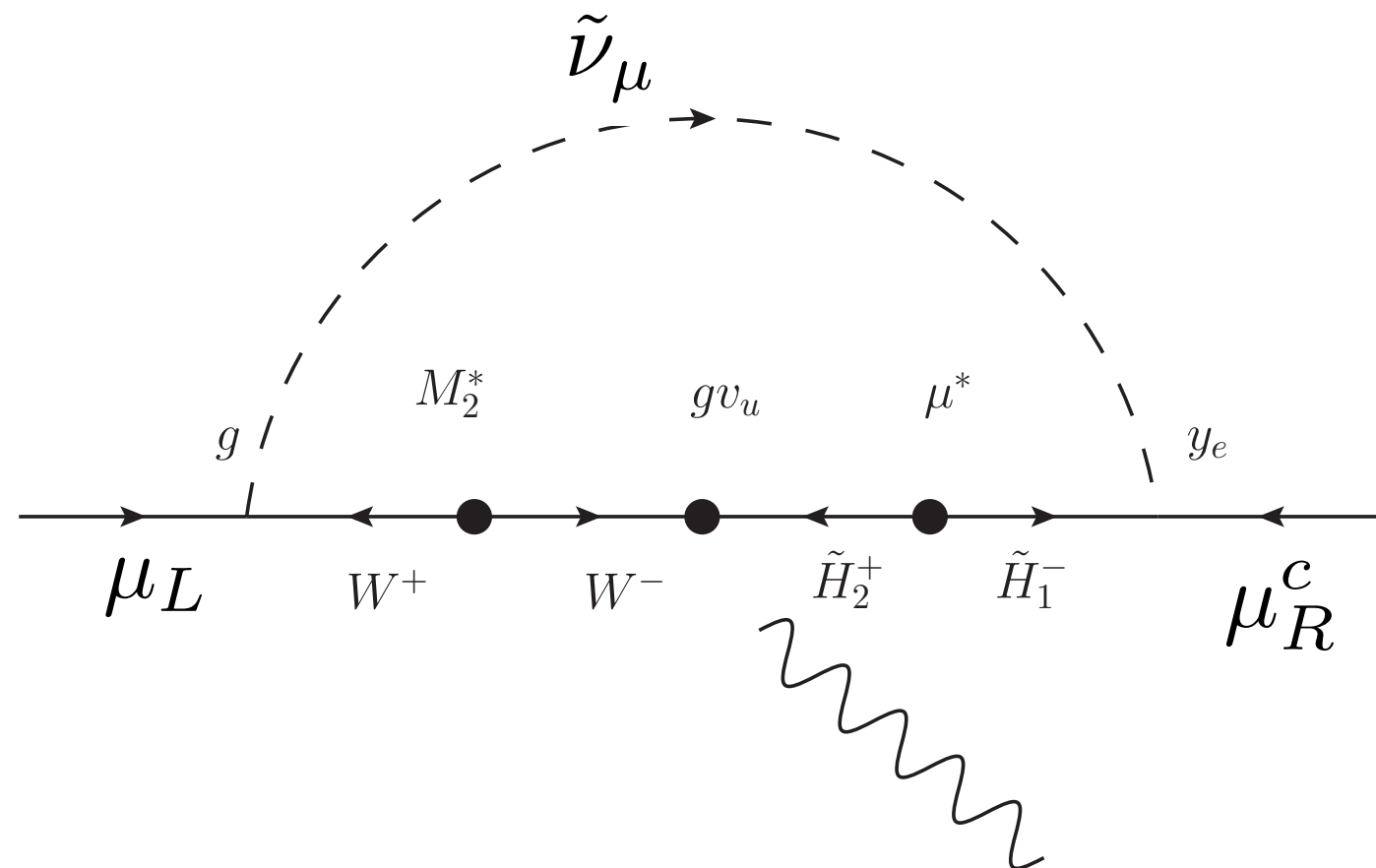
(Hagiwara, Martin, Nomura, Teubner, 2011)

The other group also reported the discrepancy more than  $3\sigma$  level

(M. Davier, A. Hoecker, B. Malaescu, Z. Zhang, 2010)

If the SUSY is responsible for the deviation of muon  $g-2$ , sleptons can not be heavy

Dominant SUSY contribution to the muon  $g-2$  is essentially same diagram as that of EDM



$$d_e \simeq \frac{m_e}{2m_\mu^2} \text{Arg}(M_2 B_\mu^*) a_\mu^{\text{SUSY}} \quad (\text{J. L. Feng, T. Moroi, 1999})$$

To suppress the EDM while explaining the muon  $g-2$  is quite difficult





$$\text{Arg}(B_\mu)$$

$\mu/B_\mu$  have to be induced with the phase smaller than  $O(10^{-3} - 10^{-4})$

(e.g.) Only SUSY mass,  $\mu$  is generated above the messenger scale

$$W = \lambda \frac{X^2}{M_P} H_u H_d \quad \begin{array}{l} \text{PQ breaking scale} \\ 10^9 \text{ GeV} \lesssim \langle X \rangle \lesssim 10^{12} \text{ GeV} \end{array}$$

However,  $O(10^{-3} - 10^{-4})$  phase can arise in other ways

The CPV effects from Dim.  
5 GUT breaking operator

24 Higgs case

$$SU(5) \xrightarrow{\langle \Sigma \rangle} SU(3)_C \times SU(2)_L \times U(1)_Y$$

# 24 Higgs breaks GUT symmetry

$$\langle \Sigma \rangle = \frac{v_{24}}{2\sqrt{15}} \text{diag}(2, 2, 2, -3, -3)$$

Messenger

dim. 5

(The GUT breaking SUSY mass term may also exist)

$$\begin{aligned} W &= \lambda_0 S \bar{\Psi}^\alpha \Psi_\alpha + \frac{\lambda_1}{M_{\text{Pl}}} S \bar{\Psi}^\alpha \Sigma_\alpha^\beta \Psi_\beta + M \bar{\Psi}^\alpha \Psi_\alpha \\ &= \lambda_0 \left( 1 + \frac{1}{\sqrt{15}} \epsilon_{24} \right) S \bar{\psi}_d \psi_d + \lambda_0 \left( 1 - \frac{3}{2\sqrt{15}} \epsilon_{24} \right) S \bar{\psi}_l \psi_l + \dots \end{aligned}$$

complex

$$\epsilon_{24} = \frac{\lambda_1 v_{24}}{\lambda_0 M_{\text{Pl}}} \sim \mathcal{O}(10^{-2})$$

The messengers of SU(2) doublet and SU(3) triplet have different phases of  $\mathcal{O}(10^{-3})$

The phases of gauginos are not aligned  
any more

$$M_1 = \frac{g_1^2}{16\pi^2} \left( 1 - \frac{1}{2\sqrt{15}} \epsilon_{24} \right) \frac{F_S}{M}$$

$$M_2 = \frac{g_2^2}{16\pi^2} \left( 1 - \frac{3}{2\sqrt{15}} \epsilon_{24} \right) \frac{F_S}{M}$$

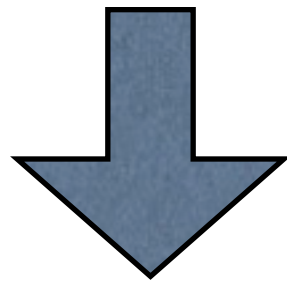
$$M_3 = \frac{g_2^2}{16\pi^2} \left( 1 + \frac{1}{\sqrt{15}} \epsilon_{24} \right) \frac{F_S}{M}$$

$$\boxed{\text{complex}} \quad \epsilon_{\mathbf{24}} = \frac{\lambda_1 v_{\mathbf{24}}}{\lambda_0 M_{\text{Pl}}} \sim \mathcal{O}(10^{-2})$$

The phases differ by  $\mathcal{O}(10^{-3})$

The Higgs B-term is also affected by the phase difference of gauginos through RGE

$$\frac{dB_\mu}{d\ln\mu} = \frac{1}{8\pi^2} \left[ 3g_2^2 M_2 + g_1^2 M_1 - 3\text{tr}(Y_U^\dagger A_U) - 3\text{tr}(Y_D^\dagger A_D) - \text{tr}(Y_L^\dagger A_L) \right]$$



$O(10^{-3})$

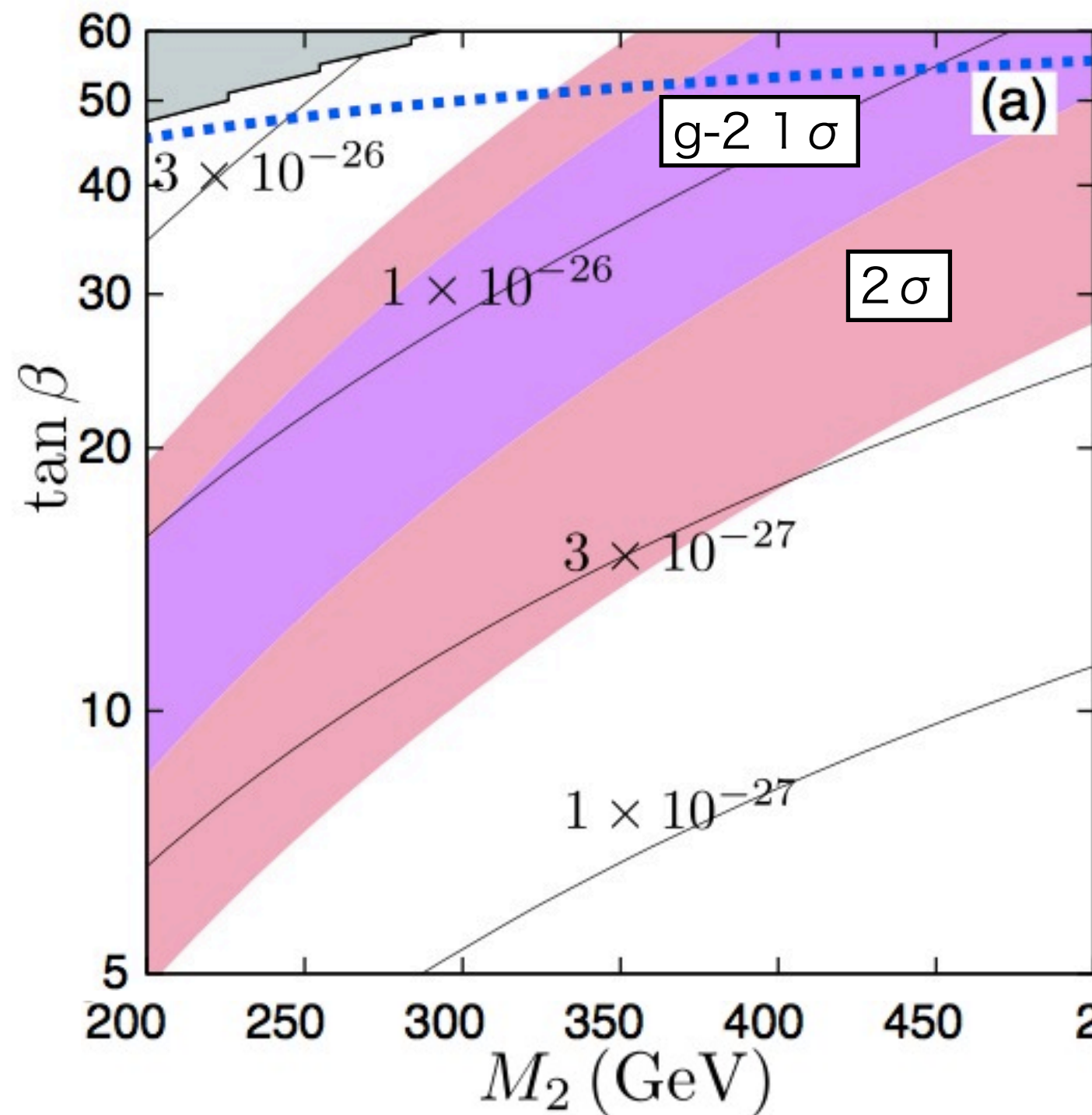
$$d_e \propto m_e \tan \beta \text{Arg}(M_2 B_\mu^*) / m_{soft}^2$$

The induced CP phase is large enough to be constrained from EDM experiments

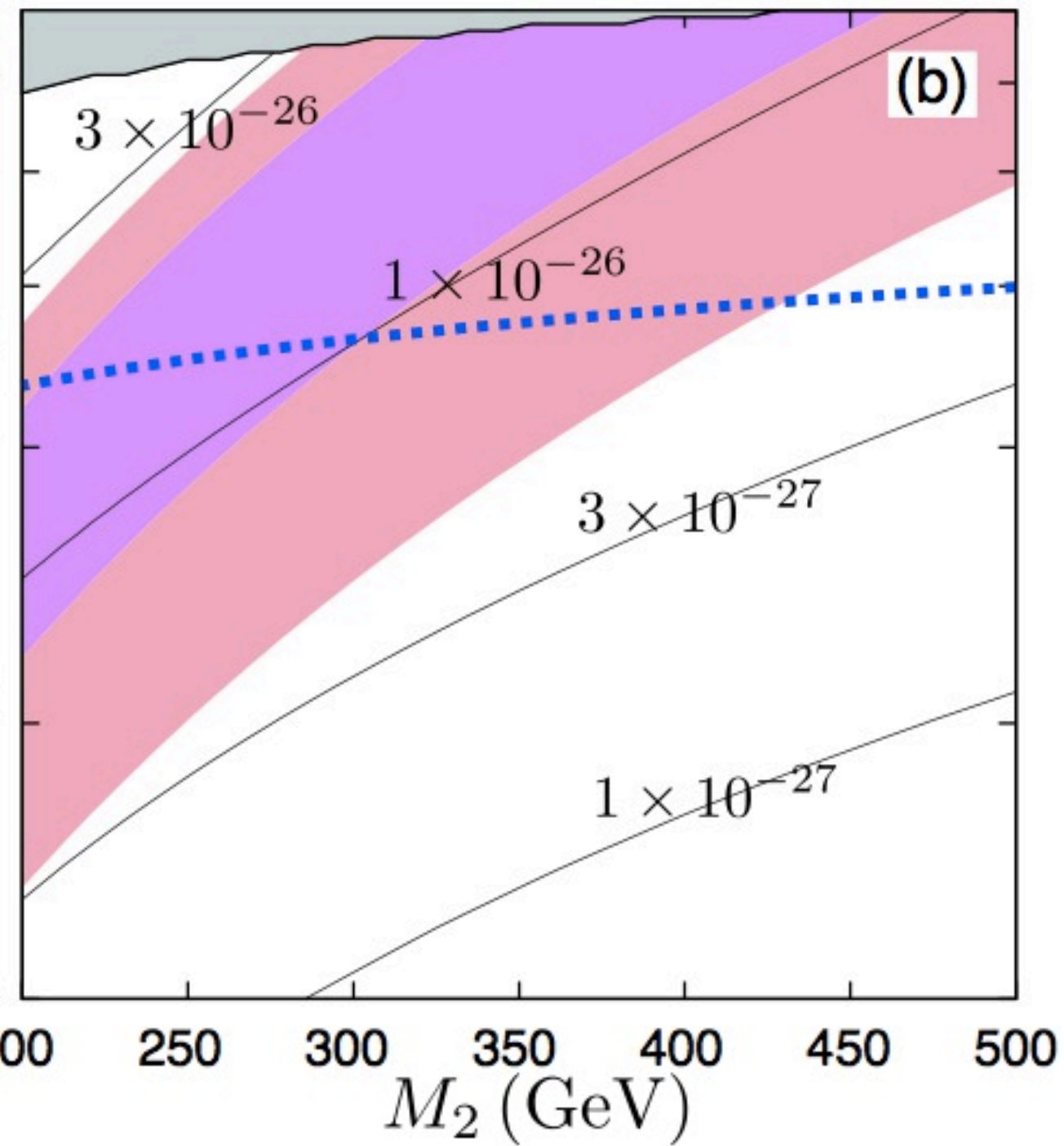
for numerical calculation  $\epsilon_{24} = i0.01$



$$M_{\text{mess}} = 10^6 \text{ GeV}$$



$$M_{\text{mess}} = 10^{12} \text{ GeV}$$



The dim 5 GUT breaking operator should be suppressed  
by  $O(0.1)$  somehow

$$\text{exp. bound } d_e < 2.1 \times 10^{-27} e \text{ cm} \quad (95\% \text{ C.L.}).$$

The CPV effects from Dim.  
6 GUT breaking operator

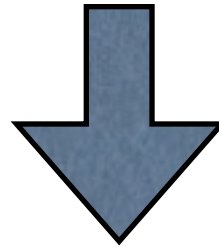
75 Higgs case

$$SU(5) \xrightarrow{\langle \Sigma \rangle} SU(3)_C \times SU(2)_L \times U(1)_Y$$

Messenger

dim. 6

$$W = \lambda_0 S \bar{\Psi}^\alpha \Psi_\alpha + \frac{\lambda_1}{M_{\text{Pl}}^2} S \bar{\Psi}^\alpha \Sigma_{\alpha\epsilon}^{\gamma\delta} \Sigma_{\gamma\delta}^{\beta\epsilon} \Psi_\beta + M \bar{\Psi}^\alpha \Psi_\alpha$$



$$\epsilon_{75} = \frac{\lambda_1^{1/2} v_{75}}{\lambda_0^{1/2} M_{\text{Pl}}}$$

$$M_A = \frac{g_A^2}{16\pi^2} (1 + \kappa_A^{(75)} \epsilon_{75}^2) \Lambda,$$

$$\kappa_1^{(75)} = \frac{11}{60}, \kappa_2^{(75)} = \frac{1}{4}, \kappa_3^{(75)} = \frac{1}{12}.$$

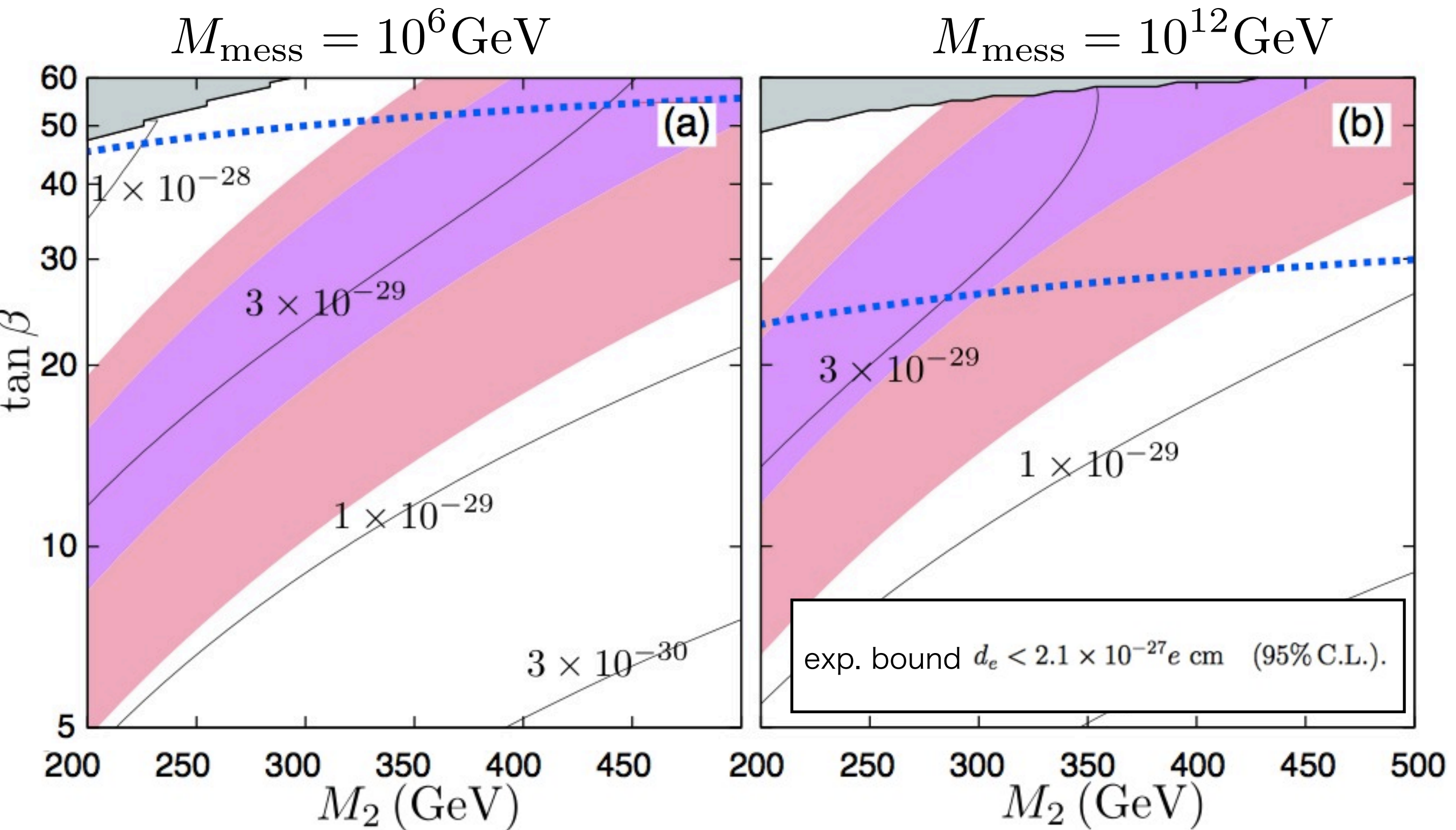
The induced CP phase

$O(10^{-5})$

$$d_e \propto m_e \tan \beta \text{Arg}(M_2 B_\mu^*) / m_{\text{soft}}^2$$

for numerical calculation  $\epsilon_{75} = i0.01$





The dim 6 GUT breaking operator is consistent with  
g-2 and EDM  
EDM may be seen at the future experiment

# The SUGRA effects

- Even in GMSB, the effects from SUGRA exists
- Higgs B-term obtains additional contribution from SUGRA

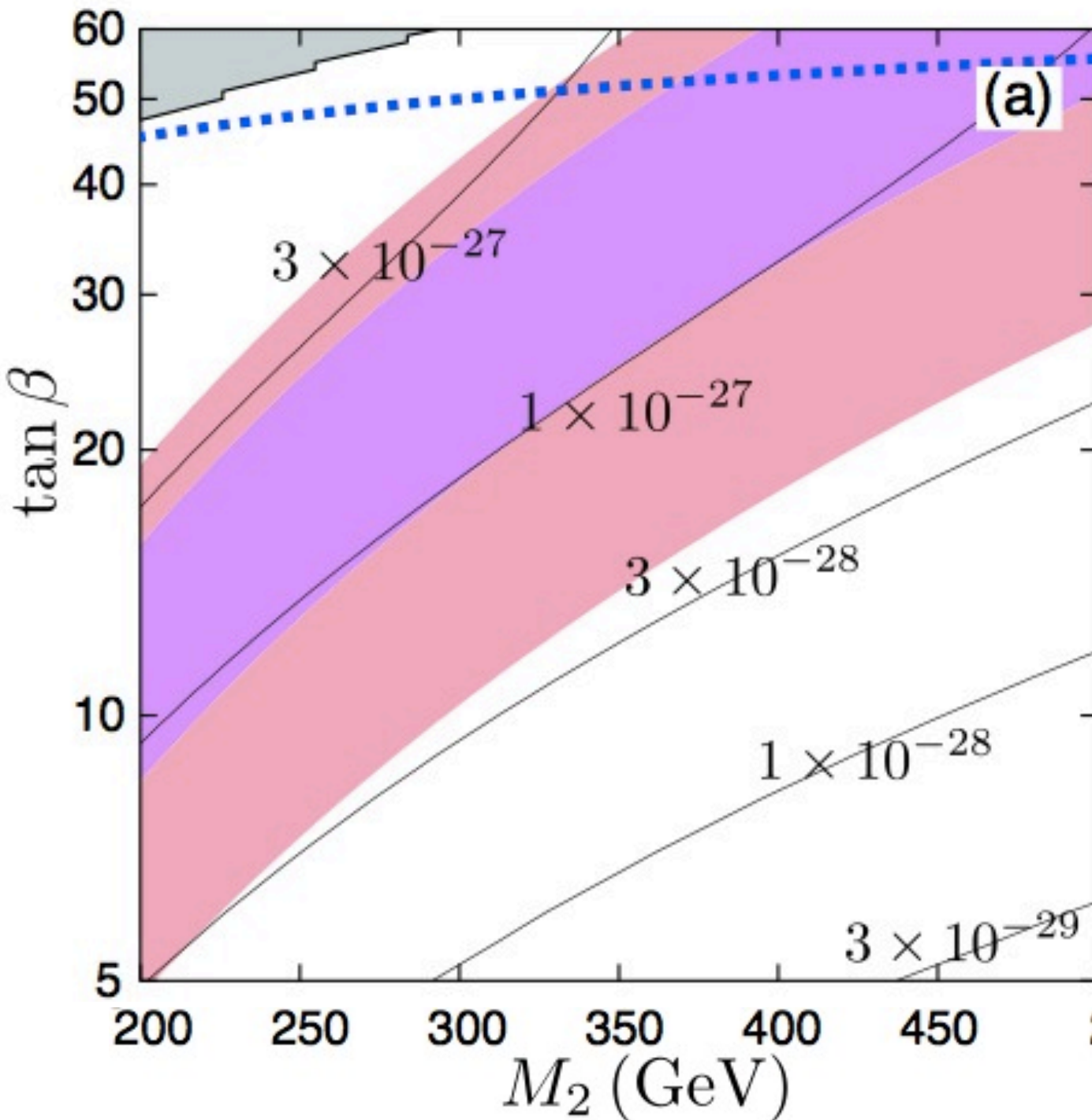
$$B_{\mu} = B_{\mu}^{(0)} + B_{\mu}^{(\text{SUGRA})} \swarrow \boxed{\text{complex}}$$

$$B_{\mu}^{(\text{SUGRA})} \sim m_{3/2}$$

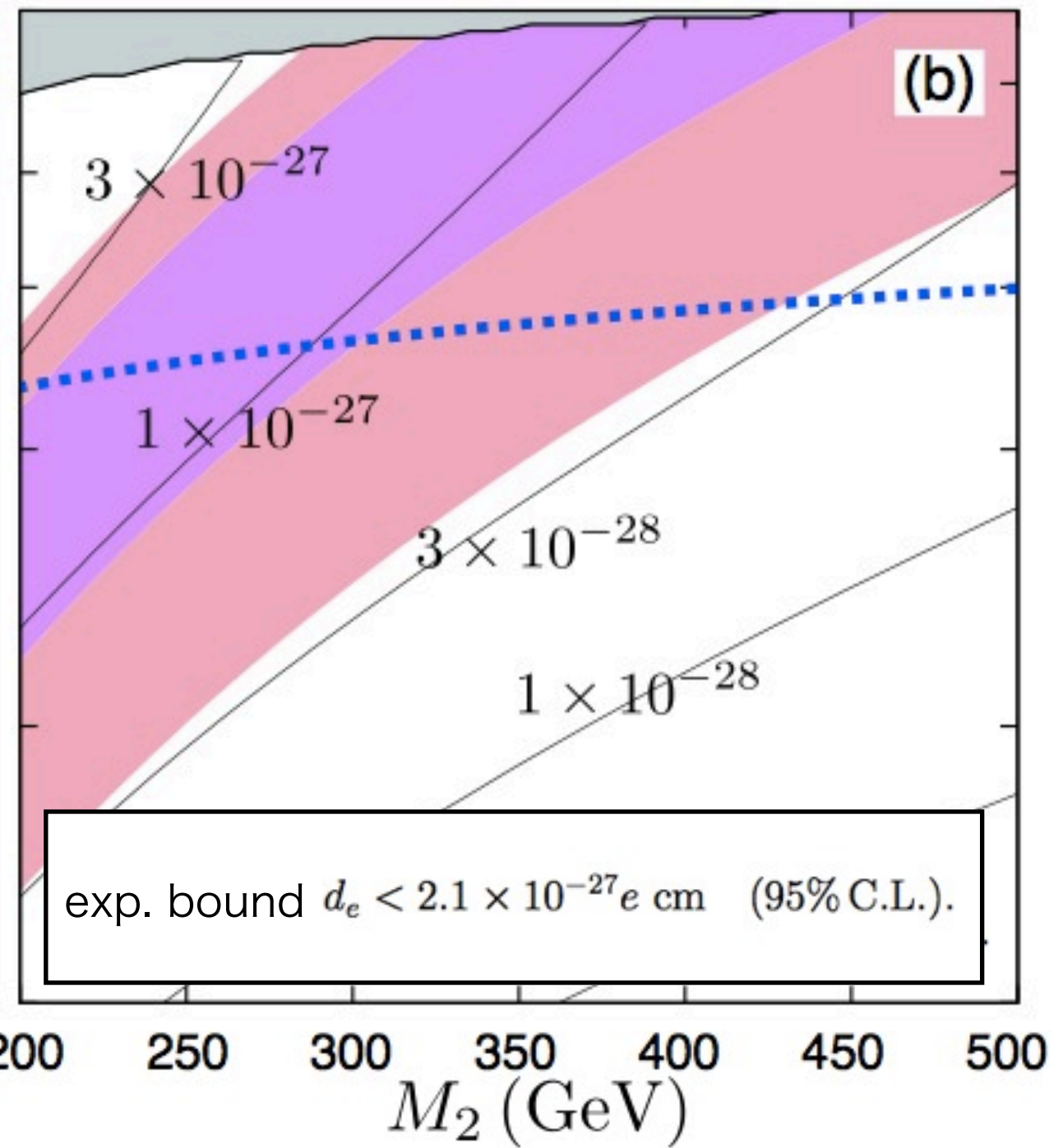
For numerical calculation, we take

$$B_{\mu}^{(\text{SUGRA})} = i100\text{MeV}$$

$$M_{\text{mess}} = 10^6 \text{ GeV}$$



$$M_{\text{mess}} = 10^{12} \text{ GeV}$$

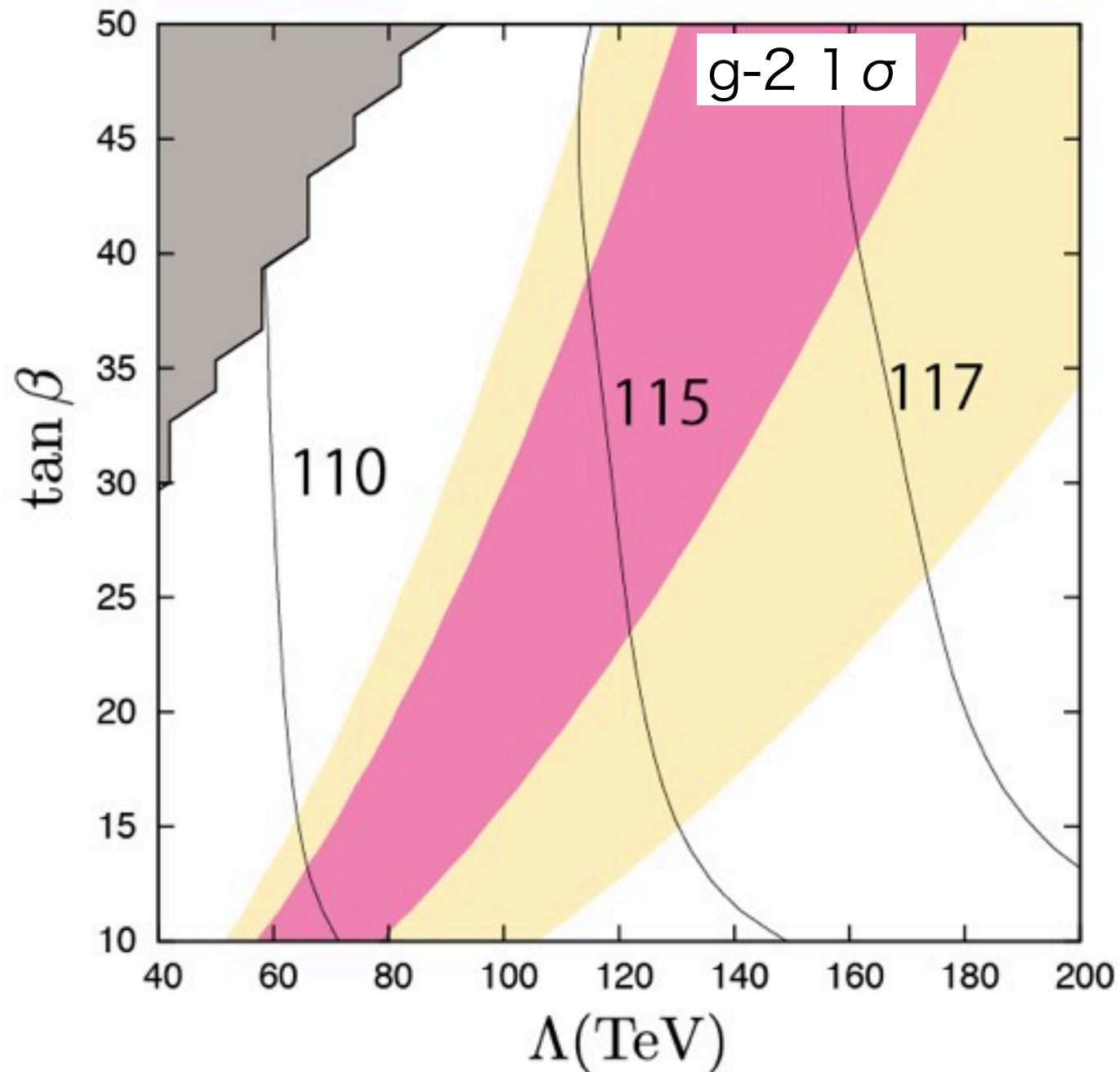


100 MeV gravitino is marginally consistent  
with g-2 and EDM

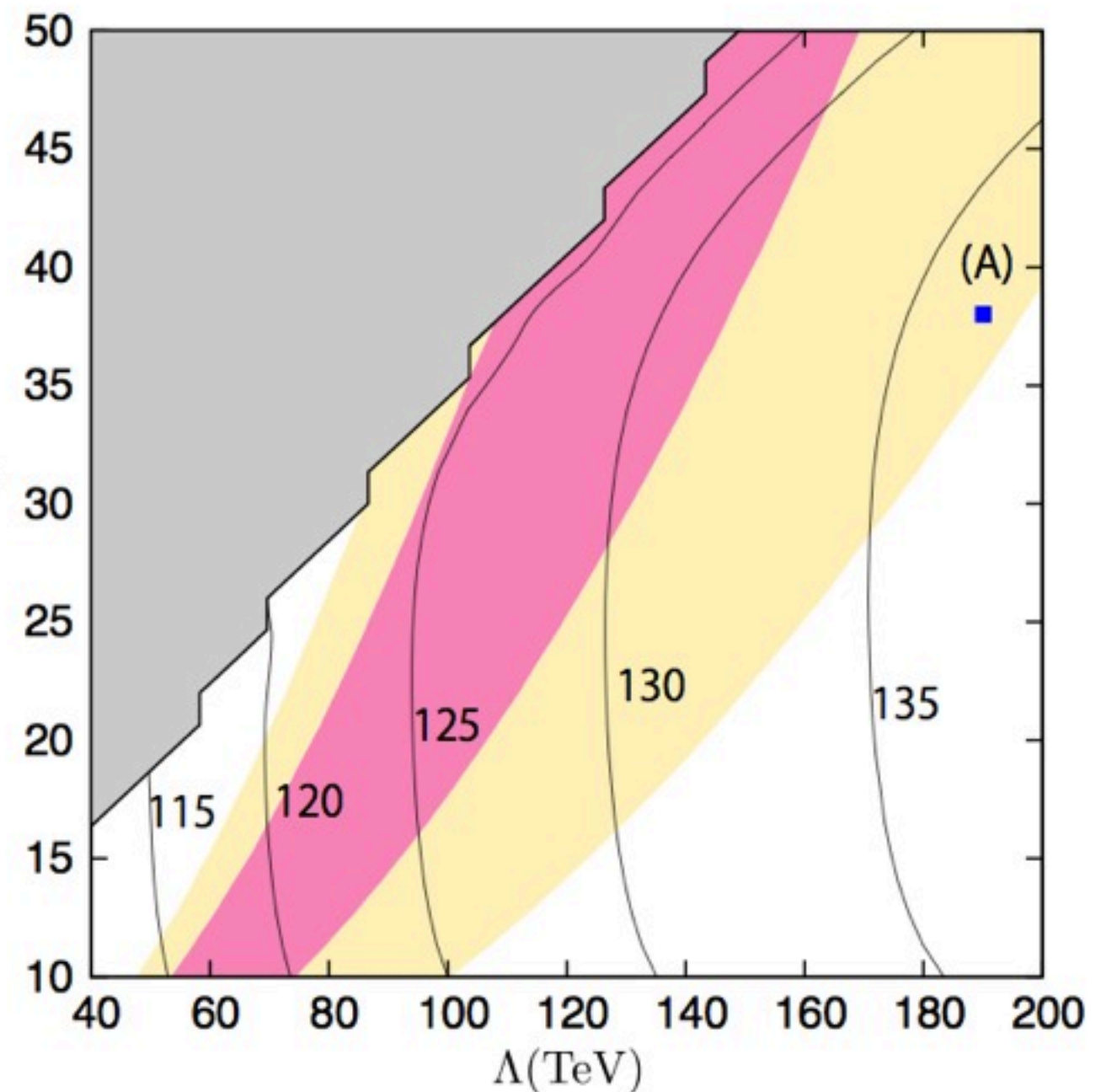


# Higgs mass in minimal GMSB

$$M_{\text{mess}} = 5 \times 10^5 \text{ GeV} \text{ and } N_5 = 1$$



MSSM



With extra vector-like matter

(M. Endo, K. Hamaguchi, S. Iwamoto, N. Yokozaki, 2011)

# Summary

- The effects of the GUT breaking operator is sizable, and may induce large EDM
- The effect of gravity mediation is also sizable when the gravitino mass is large as  $100\text{MeV}$
- EDM may be seen at future experiments